



## HOLY MISSION HIGH SCHOOL, SAMASTIPUR

Affiliated to CBSE. DELHI, +2 level

**SUBJECT- MATHS**

**CLASS-X**

### HALF YEARLY EXAMINATION-2019

**General instructions**

- 1-All questions are compulsory
- 2-The paper consists of 30 questions divided into four sections A, B, C, D
- 3-Section A comprises of 6 questions of 1 marks. Section B comprises of 6 questions of 2 marks. Section C comprises of 10 questions of 3 marks. Section D comprises of 8 questions of 4 marks.
4. Use of calculator is not permitted

#### SECTION-A

1. Two different dice are tossed together. Find the probability that the product of the two numbers on the top of the dice is 6.
2. If the sum of the zeroes of the polynomial  $f(x) = 2x^3 - 3kx^2 + 4x - 5$  is 6, then find the value of  $k$
3. State Euclid's division lemma
4. If  $\Delta ABC \sim \Delta PQR$ ,  $BC = 8$  cm and  $QR = 6$  cm, find the ratio of the areas of  $\Delta ABC$  and  $\Delta PQR$
5. Find the nature of roots of the quadratic equation  $2x^2 - 4x + 3 = 0$ .
6. Find the value of  $(\sec^2 A - 1) \cdot \cot^2 A$

#### SECTION-B

7. Using Euclid's division algorithm, find the HCF of 2160 and 3520.
8. Find the zeroes of the quadratic polynomial  $5t^2 + 12t + 7$  and verify the relationship between the zeroes and the coefficients.
9. Take  $A = 60$  and  $B = 30$ . Write the value of  $\cos A$ ,  $\cos B$  and  $\cos(A+B)$ . Is  $\cos(A+B) = \cos A + \cos B$
10. Find the value of  $k$  if the points  $A(2, 3)$ ,  $B(4, k)$  and  $C(6, -3)$  are collinear.
11. Write down the decimal expansion of  $76/6250$ , without actual division.
12. If  $\sec A + \tan A = m$  and  $\sec A - \tan A = n$ , find the value of  $mn$ .

#### SECTION-C

13. Find all the zeroes of the polynomial  $x^4 - 3x^3 + 6x - 4$ , if two of zeroes are  $\sqrt{2}$  and  $-\sqrt{2}$
14. Solve  $2x + 3y = 11$  and  $2x - 4y = -24$  and hence find the value of 'm' for which  $y = mx + 3$ .
15. Prove that  $\sqrt{5}$  is an irrational number.
16. If  $(1, 2)$ ,  $(4, y)$ ,  $(x, 6)$  and  $(3, 5)$  are the vertices of a parallelogram taken in order, find  $x$  and  $y$ .
17. Find the roots of the equation  $5x^2 - 6x - 2 = 0$ , by method of completing the square.

$$\frac{1}{1} + \frac{1}{1} = 2 \operatorname{cosec} A \cot A$$

#### 18. $\sec A - 1$    $\sec A + 1$

19. Find the relation between  $x$  and  $y$  if points  $(2, 1)$ ,  $(x, y)$  and  $(7, 5)$  are collinear.
20.  $ABC$  is a right triangle, right angled at  $A$ , and  $D$  is the mid-point of  $AB$ . Prove that  $BC^2 = CD^2 + 3BD^2$ .



21.  $ABCD$  is a trapezium in which  $AB \parallel DC$  and its diagonals intersect each other at the point  $O$ . Show  $\frac{AO}{BO} = \frac{CO}{DO}$ .

22. Solve for  $x$ :

$$\frac{1}{a+b+x} = \frac{1}{a} + \frac{1}{b} + \frac{1}{x}; a \neq 0, b \neq 0, x \neq 0$$

#### SECTION-D

23. Prove that "The ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides."
24. The sum of the reciprocals of Rehman's ages, (in years) 3 years ago and 5 years from now is  $\frac{1}{3}$ . Find his present age.
25.  $ABC$  is a triangle in which  $AB = AC$  and  $D$  is any point in  $BC$ . Prove that :  $(AB)^2 - (AD)^2 = BD \cdot CD$ .



26. A student noted the number of cars passing through a spot on a road for 100 periods each of 3 minutes and summarised it in the table given below. Find the mode of the data:

Number of cars	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
Frequency	17	14	13	22	20	11	15	8

27. A number is a two digit number which is three times more than 4 times the sum of the digits. If 18 is added to the number, the digits gets opposite. Represent geometrically

28. If the polynomial  $x^4 - 6x^3 + 16x^2 - 25x + 10$  is divided by another polynomial  $x^2 - 2x + k$ , the remainder comes out to be  $(x + \alpha)$ , find  $k$  and  $\alpha$ .

29. A bag contains tickets, numbered 11, 12, 13, ..., 30. A ticket is taken out from the bag at random. Find the probability that the number on the drawn ticket

- (i) is a multiple of 7 (ii) is greater than 15 and a multiple of 5
30. If A(-4, 8), B(-3, -4), C(0, -5) and D(5, 6) are the vertices of a quadrilateral ABCD, find its area

**ALL THE BEST**