

# CENTRAL PUBLIC SCHOOL

Subject - Maths

TAJPUR ROAD, SAMASTIPUR

Time - 3 hrs.

Class - IX

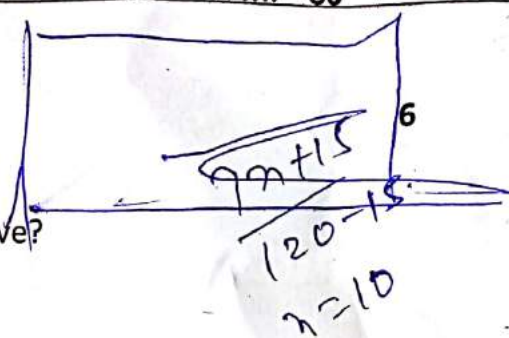
MID TERM EXAM - 2018

F. M. - 80

## Section - A

Solve these sums.

1. If  $625^x = \frac{25}{5^x}$ , Find x..
2. In which quadrant (s), the abscissa of a point is negative?
3. Find the value of  $f(x) = 2x^2 + 7x + 3$  at  $x = -2$ .
4. To which country does Euclid belong?
5. Find the measure of an angle whose supplement is equal to the angles itself.
6. Find the area of an isosceles triangle having base x cm and equal side y cm.



## Section - B (2marks each)

7. Factorise :  $7\sqrt{2}x^2 - 10x - 4\sqrt{2}$
8. Find the angle which exceeds its complement by  $20^\circ$ .
9. It is known that  $x + y = 10$  and that  $x = z$ . Show that  $z + y = 10$ . Solve the equation using appropriate Euclid's axiom.
10. The diagonals of a rectangle ABCD meet at O. If  $\angle BCD = 44^\circ$ , find  $\angle OAD$ .
11. The altitude of an equilateral triangle is  $3\sqrt{3}$  cm. Find its area.
12. If the mean of the observations  $x, 2x+1, 2x+5, 2x+9$  is 30, what is the mean of last two observations.

Value  
 $2x+5$   
 $2x+15$   
 $30+5$   
 $35$   
 $2x+15+9$   
 $34+9$   
 $43$

## Section - C (3 marks each)

13. If  $x = 5 - 2\sqrt{6}$  then find the value of  $x^2 + \frac{1}{x^2}$
14. Verify that :  $x^3 + y^3 + z^3 - 3xyz = \frac{1}{2}(x+y+z)[(x-y)^2 + (y-z)^2 + (z-x)^2]$
15. If  $a + b + c = 5$  and  $ab + bc + ca = 10$ , then prove that  $a^3 + b^3 + c^3 - 3abc = -25$

Or

If  $a, b, c$  are all non-zero and  $a + b + c = 0$ , prove that  $\frac{a^2}{bc} + \frac{b^2}{ca} + \frac{c^2}{ab} = 3$

16. Find the coordinates of the point.

- a. Which lies on both the axes?
- b. Whose abscissa is  $-4$  and lies on x-axis?
- c. Whose ordinate is  $5$  and lies on y-axis?

17. In  $\triangle ABC$ , the side AB and AC of  $\triangle ABC$  are produced to points E and D respectively. If bisectors BO and CO of  $\angle CBE$  and  $\angle BCD$  respectively meet at point O, then prove that  $\angle BOC = 90^\circ - \frac{1}{2} \angle A$ .



9.  $x = z$  (given)  
 $x + y = 10$   
 $z + y = 10$   
 (same thing which are equal to one another)  
 Maths  
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18. The mid-points of the sides of a quadrilateral are joined in order, prove that the area of the ||gm so formed will be half of the area of the given quadrilateral.

19. ABCD is a rectangle in which diagonal AC bisects  $\angle A$  as well as  $\angle C$ . Show that ABCD is square.

20. Factorise:  $2x^3 - 3x^2 - 17x + 30$  or if  $x^2 + \frac{1}{x^2} = 34$ , find  $x^3 + \frac{1}{x^3} - 9$

21. The unequal side of an isosceles triangle measures 24cm and its area is  $60\text{cm}^2$ . Find the perimeter of the given isosceles triangle.

22. The mean of the following distribution is 50.

x	10	30	50	70	90
F	17	$5a + 3$	32	$7a - 11$	19

Find the value of a and hence the frequencies of 30 and 70.

### Section - D (4 marks each)

23. Represent  $\sqrt{4.5}$  on the number line. With steps.

24. Find the values of a and b so that  $(z+1)$  and  $(z-1)$  are factors of  $z^4 + az^3 + 2z^2 - 3z + b$ .

Or

Prove that  $(a + b + c)^3 - a^3 - b^3 - c^3 = 3(a + b)(b + c)(c + a)$

25.  $\triangle ABC$  is an isosceles triangle in which  $AB=AC$ . Side BA is produced to D such that  $AD=AB$ . Show that  $\angle BCD$  is a right angle.

26. ABCD is a trapezium in which  $AB \parallel CD$  and  $AD=BC$ . Show that.

- a.  $\angle A = \angle B$       c.  $\angle C = \angle D$       d.  $\triangle ABC \cong \triangle BAD$   
 b. diagonal AC = diagonal BD.

Or

AD is the median of  $\triangle ABC$ . E is mid-point of AD. BE produced to meet AC at F. show that  $AF = \frac{1}{3} AC$ .

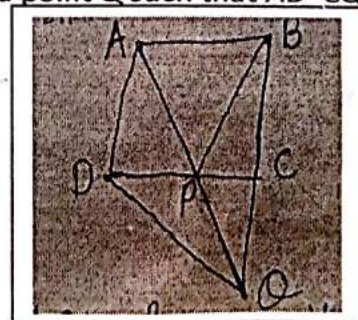
27. State and prove SSS congruence rule.

28. Draw a frequency polygon to represent the following information:

Class	25-29	30-34	35-39	40-44	45-49	50-54
frequency	5	15	23	20	10	7

29. In figure ABCD is a parallelogram and BC is produced to a point Q such that  $AD=CQ$ . If AQ intersect DC at P, show that  $\text{ar}(BPC) = \text{ar}(DPQ)$ .

(11) Altitude of a equilateral triangle is  $\frac{\sqrt{3}}{2}$   
 $3\sqrt{3} = \frac{\sqrt{3}a}{2}$   
 $\sqrt{3}a = 6\sqrt{3}$



30. Prove that sum of any two sides of a triangle is greater than twice the median with respect to the third side.

Or

In a  $\square ABCD$  in which diagonal AC and BD intersect at O, show that  $AB + BC + CD + DA < 2(AC + BD)$