

साधना देवी विद्यापीठ

Punjabi Colony (Dharampur) Samastipur. 848101 (Bihar)
Half Yearly Examination-2019-20

Class :- IX
Sub :- Maths

Time :- 3hrs
F.M. :- 100

General Instructions

- Section A contains 9 questions of 1 mark each.
- Section B contains 9 questions of 3 marks each.
- Section C contains 8 questions of 5 marks each.
- Section D contains 4 questions of 6 marks each.

20 x 1 = 20
2 x 6 = 12
3 x 8 = 24
4 x 6 = 24

Section - A

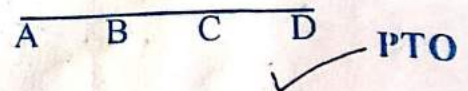
* Tick the correct option :-

1. Which of the following is a rational number?
(a) $1 + \sqrt{3}$ (b) π (c) $2\sqrt{3}$ (d) 0
2. Which of the following is an irrational?
(a) $\sqrt{23}$ (b) $\sqrt{225}$ (c) 0.3799 (d) $7.\overline{478}$
3. If $(x+1)$ is a factor of the polynomial $(2x^2 + Kx)$ then the value of K is
(a) -2 (b) -3 (c) 2 (d) 3
4. If $\frac{a}{b} + \frac{b}{a} = -1$ then $(a^3 - b^3) = ?$
(a) -3 (b) -2 (c) -1 (d) 0
5. If $(2, 0)$ is a solution of the linear equation $2x + 3y = K$ then the value of K is
(a) 6 (b) 5 (c) 9 (d) 4
6. If the point $(3, 4)$ lies on the graph of $3y = ax + 7$ then the value of a is
(a) $\frac{2}{5}$ (b) $\frac{5}{3}$ (c) $\frac{3}{5}$ (d) $\frac{2}{7}$
7. The ordinate of every point on the x-axis is
(a) 1 (b) -1 (c) 0 (d) any real number
8. An exterior angle of a triangle is 110° and its two interior opposite angle are equal. Each of these equal angle is.
(a) 70° (b) 55° (c) 35° (d) $24\frac{1}{2}^\circ$
9. In ΔABC $\angle A = 40^\circ$ $\angle B = 60^\circ$ Then the longest side of ΔABC is
(a) BC (b) AC (c) AB (d) Cannot be determined.

Section - B

Solve the following

10. Locate $\sqrt{3}$ on the number line. ✓
11. Find the remainder when $x^3 + 3x^2 + 3x + 1$ is divided by $(x - \frac{1}{2})$ ✓
12. Factorise $12x^2 - 7x + 1$ ✓
13. Locate the points on the cartesian plane $(-2, 4)$, $(3, -1)$ and $(-1, 0)$
14. The taxi fare in a city is as follows. for the first kilometre, the fare is Rs. 8 and for the subsequent distance it is Rs. 5 per km taking distance covered as x km and total fare as Rs y write linear equation for this information and draw its graph.
15. In the given figure $AC = BD$ then prove that $AB = CD$ ✓

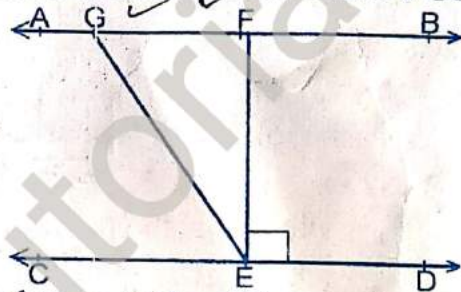


PTO

16. If two lines intersect each other then prove that vertically opposite angles are equal. ✓
 17. Lines which are parallel to the same lines are parallel to each other prove it. ✓
 18. Show that in a right angled triangle the hypotenuse is the longest side. ✓

Section C

19. Solve :-
 Prove that the sum of any two sides of a triangle is greater than the third side.
 20. ΔABC is an isosceles triangle in which $AB=AC$ side BA is produced to D such that $AD=AB$. Show that $\angle BCD$ is a right angle.
 21. In right triangle ABC right angled at C M is the mid point of hypotenuse AB C is joined to M and produced to a point D such that $DM = CM$ point D is joined to point B . Show that.
 (a) $\angle DBC$ is a right angle. (b) $CM = \frac{1}{2} AB$
 22. The side QR of ΔPQR is produced to a point S if the bisectors of $\angle PQR$ and $\angle PRS$ meet at point T . Then prove that $\angle QTR = \frac{1}{2} \angle QPR$ (Draw figure).
 23. If $AB \parallel CD$, $EF \perp CD$ and $\angle GED = 126^\circ$, Find $\angle AGE$, $\angle GEF$ and $\angle FGE$.

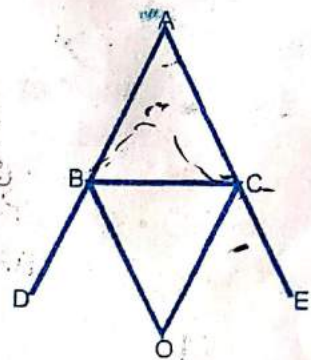


Handwritten algebraic identities:
 $(a+b)^2 = a^2 + b^2 + 2ab$
 $(a-b)^2 = a^2 + b^2 - 2ab$
 $(a+b)(a-b) = a^2 - b^2$

24. Prove that every line segment has one and only one mid point.
 25. Prove that $x^3+y^3+z^3 - 3xyz = \frac{1}{2}(x+y+z) [(x-y)^2 + (y-z)^2 + (z-x)^2]$ By splitting L.H.S
 26. Factorise $x^3-23x^2+142x-120$ by using factor theorem.

Section D

27. In a ΔABC the sides AB and AC are produced to points D and E respectively. The bisectors of $\angle DBC$ and $\angle ECB$ intersect at point O . Prove that $\angle BOC = (90^\circ - \frac{1}{2}A)$



28. Prove that sum of all angles around a point is 360° .
 29. Prove that the perimeter of a triangle is greater than the sum of its three medians.
 30. In a quadrilateral $ABCD$ the line segment bisecting $\angle C$ and $\angle D$ meet at E . Prove $\angle A + \angle B = 2 \angle CED$

Handwritten solution for question 30:
 $\angle C + \angle D = 360 - (\angle A + \angle B)$
 $\frac{1}{2}(\angle C + \angle D) = \frac{1}{2}(360 - (\angle A + \angle B))$
 $\angle CED = 180 - \frac{1}{2}(\angle C + \angle D)$
 $\angle CED = 180 - \frac{1}{2}(360 - (\angle A + \angle B))$
 $\angle CED = 180 - 180 + \frac{1}{2}(\angle A + \angle B)$
 $\angle CED = \frac{1}{2}(\angle A + \angle B)$
 $2 \angle CED = \angle A + \angle B$